

# Symmetry in Nature: Discreteness, Three-Dimensional Extension and Minimum Potential Energy

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**Abstract.** At every scale of Nature symmetry manifests in a variety of ways, leading over the centuries to apparently disjoint descriptions, from Platonic solids, through Fibonacci numbers, to charge, parity, and time invariance. It is claimed that discreteness, three-dimensional extension, and minimization of potential energy may be the common basic principles leading to observed symmetries. The author found (Nature 1986) that punctual  $N$  discrete masses array on the surface and inside a sphere in highly symmetrical configurations exhibiting tangential equilibrium and low potential energy in an inverse potential field. Present paper adds new boundary conditions arising from the three-dimensional extension of the discrete masses, and from the rotational motion of the symmetrical  $N$ -particle arrays ( $1 < N < 21$ ).